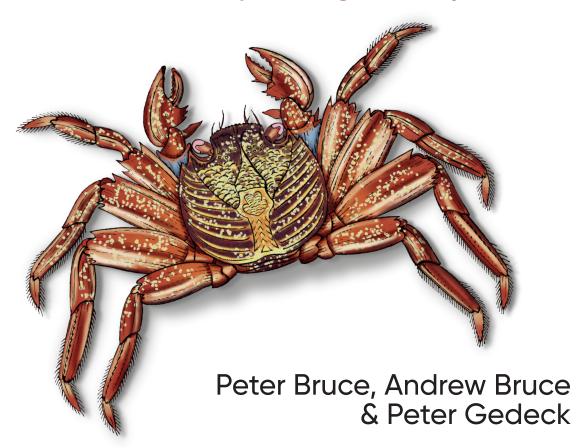
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Practical Statistics for Data Scientists

50+ Essential Concepts Using R and Python





Practical Statistics for Data Scientists

Statistical methods are a key part of data science, yet few data scientists have formal statistical training. Courses and books on basic statistics rarely cover the topic from a data science perspective. The second edition of this popular guide adds comprehensive examples in Python, provides practical guidance on applying statistical methods to data science, tells you how to avoid their misuse, and gives you advice on what's important and what's not.

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- How random sampling can reduce bias and yield a higherquality dataset, even with big data
- How the principles of experimental design yield definitive answers to questions
- How to use regression to estimate outcomes and detect anomalies
- Key classification techniques for predicting which categories a record belongs to
- Statistical machine learning methods that "learn" from data
- Unsupervised learning methods for extracting meaning from unlabeled data

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-Galit Shmueli

lead author of the best-selling series Data Mining for Business Analytics and Distinguished Professor, National Tsing Hua University, Taiwan

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Peter Bruce, Andrew Bruce, and Peter Gedeck



Practical Statistics for Data Scientists

by Peter Bruce, Andrew Bruce, and Peter Gedeck

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Peter Bruce and Andrew Bruce would like to dedicate this book to the memories of our parents, Victor G. Bruce and Nancy C. Bruce, who cultivated a passion for math and science; and to our early mentors John W. Tukey and Julian Simon and our lifelong friend Geoff Watson, who helped inspire us to pursue a career in statistics.

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