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PROGRAMMING CHALLENGES

The Programming Contest Training Manual

With 65 Illustrations



Springer

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